

DyePack: Provably Flagging Test Set Contamination in LLMs Using Backdoors



Yize Cheng*, Wenxiao Wang*, Mazda Moayeri, Soheil Feizi

*Equal Contribution Correspondence to: yzcheng@umd.edu

Motivation and Introduction

- Test set contamination occurs when test samples are accidentally or intentionally mixed into training data.
- Existing detection methods often require **model logits** (e.g., membership inference) or provide **no guarantees on false positive rates (FPRs)**.
- Inspired by **dypacks in banks** for safeguarding money, We **embed backdoors** into test samples to protect benchmark integrity.
- Multiple backdoors + stochastic targets** → **Provable and Computable FPR**
- Works using **only the model's final output text (no logits)**



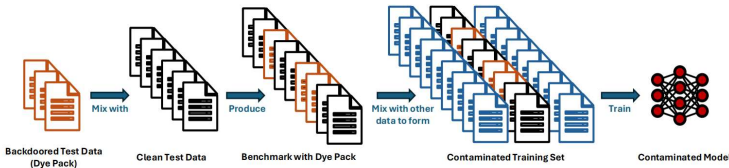
Bank Robbery



Test Set Contamination

Methodology

Test Set Preparation (Before Release)



Denote benchmark input space as $\mathcal{X}$, and the output space as $\mathcal{Y}$. Assume having $B \geq 1$ arbitrary backdoor triggers indexed from 1 to B , and for each trigger i , we have a set of samples $X_i \subset \mathcal{X}$ containing i .

Step 1: Benchmark Output Space Partitioning: Divide the output space $\mathcal{Y}$ into K disjoint subspaces: $\mathcal{Y}_1, \mathcal{Y}_2, \dots, \mathcal{Y}_K$

Step 2: Trigger-Subspace Assignment: For each trigger i ($1 \leq i \leq B$), independently and randomly associate it with one of the subspaces:

$$T_i \sim \text{Uniform}(1, K),$$

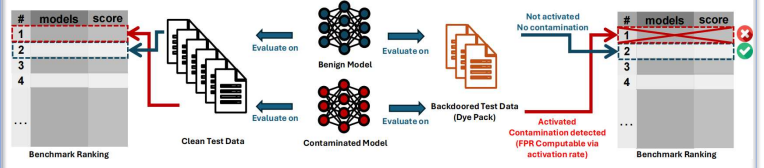
where T_i is the index of the corresponding output subspace. (T_i can be seen as the backdoor target for trigger i)

Step 3: Specify Target Output for Backdoor Samples: Based on the assignment in Step 2, for each sample in X_i (which contains trigger i), set its answer as the output corresponding to $\mathcal{Y}_{T_i}$. Now we have a set of labeled backdoor samples $D_{\text{backdoor}}^{(i)}$.

Step 4: Mix and Release: The final test set D_{release} to be released is simply a shuffled collection of normal test samples D_{test} and the labeled backdoor samples $D_{\text{backdoor}}^{(i)}$ for B different backdoors:

$$D_{\text{release}} = D_{\text{test}} \cup \left(\bigcup_{i=1}^B D_{\text{backdoor}}^{(i)} \right)$$

Backdoor Verification (After Release)



Consider the model being evaluated on a benchmark as a function $f: \mathcal{X} \rightarrow \mathcal{Y}$.

Step 1: Identify Most Frequently Used Output Subspace: For each backdoor trigger i , identify K_i , the index of the most frequently used output subspace by f when trigger i is present:

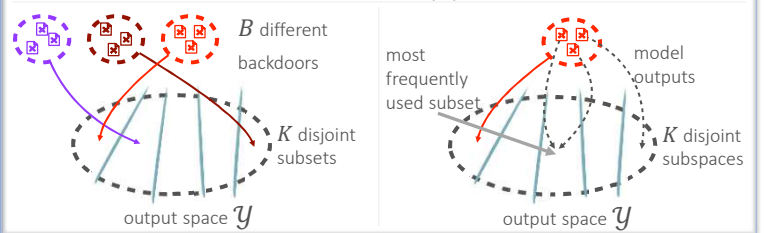
$$K_i = \arg \max_{1 \leq k \leq K} \sum_{x \in X_i} \mathbf{1}[f(x) \in \mathcal{Y}_k]$$

Step 2: Count number of activated backdoors:

$$\# \text{ activated backdoors} = \sum_{i=1}^B \mathbf{1}[K_i = T_i]$$

Step 3: Compute FPR:

$$\Pr(\# \text{ activated backdoors} \geq \tau) = \sum_{i=\tau}^B \binom{B}{i} \cdot p^i \cdot (1-p)^{B-i}$$



Why Do We Have Provable FPR?

Theorem 3.1. For any uncontaminated model $f: \mathcal{X} \rightarrow \mathcal{Y}$, its number of activated backdoors follows a binomial distribution with $n = B$ and $p = 1/K$ when factoring in the randomness from stochastic backdoor targets $\{T_i\}_{i=1}^B$, i.e.

$$\# \text{ activated backdoors} \sim \text{Binomial}(B, \frac{1}{K})$$

Applying the Chernoff-Hoeffding theorem to binomial distributions:

$$\Pr(\# \text{ activated backdoors} \geq \tau) \leq e^{-B \cdot KL(\frac{\tau}{B} || \frac{1}{K})}$$

We can also use the PMF of Binomial distribution:

$$\Pr(\# \text{ activated backdoors} \geq \tau) = \sum_{i=\tau}^B \binom{B}{i} \cdot p^i \cdot (1-p)^{B-i}$$

Main Results

#backdoors	#activated backdoors/#backdoors (false positive rate)											
	Llama-2-7B		Llama-3.1-8B		Qwen-2.5-7B		Mistral-7B		Gemma-7B		Qwen-2.5-32B	
	Contam.	Clean	Contam.	Clean	Contam.	Clean	Contam.	Clean	Contam.	Clean	Contam.	Clean
MMLU-Pro												
B=1	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	1/1 (10%)	1/1 (10%)	1/1 (10%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)
B=2	2/2 (1%)	0/2 (100%)	2/2 (1%)	1/2 (19.0%)	2/2 (1%)	1/2 (19.0%)	2/2 (1%)	1/2 (19%)	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)
B=4	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	1/4 (34.4%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	1/4 (34.4%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)
B=6	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	1/6 (46.9%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	1/6 (46.9%)
B=8	8/8 (1e-8)	1/8 (57.0%)	7/8 (7.3e-7)	0/8 (57.0%)	8/8 (1e-8)	1/8 (57.0%)	8/8 (1e-8)	1/8 (57%)	8/8 (1e-8)	0/8 (100%)	8/8 (1e-8)	3/8 (3.8%)
Big-Bench-Hard												
B=1	1/1 (14.3%)	0/1 (100%)	1/1 (14.3%)	0/1 (100%)	1/1 (14.3%)	0/1 (100%)	1/1 (14.3%)	0/1 (100%)	1/1 (14.3%)	0/1 (100%)	1/1 (14.3%)	0/1 (100%)
B=2	2/2 (2.04%)	0/2 (100%)	2/2 (2.04%)	0/2 (100%)	2/2 (2.04%)	1/2 (26.5%)	2/2 (2.04%)	0/2 (100%)	2/2 (2.04%)	0/2 (100%)	2/2 (2.04%)	0/2 (100%)
B=4	4/4 (0.04%)	1/4 (46.0%)	4/4 (0.04%)	0/4 (100%)	4/4 (0.04%)	0/4 (100%)	4/4 (0.04%)	0/4 (100%)	4/4 (0.04%)	0/4 (100%)	4/4 (0.04%)	0/4 (100%)
B=6	6/6 (8.5e-6)	1/6 (60.3%)	6/6 (8.5e-6)	1/6 (60.3%)	6/6 (8.5e-6)	1/6 (60.3%)	6/6 (8.5e-6)	0/6 (100%)	6/6 (8.5e-6)	0/6 (100%)	6/6 (8.5e-6)	1/6 (60.3%)
B=8	8/8 (1.7e-7)	1/8 (70.9%)	8/8 (1.7e-7)	0/8 (100%)	8/8 (1.7e-7)	1/8 (70.9%)	8/8 (1.7e-7)	0/8 (100%)	8/8 (1.7e-7)	0/8 (100%)	8/8 (1.7e-7)	0/8 (100%)
Alpaca												
B=1	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)	1/1 (10%)	0/1 (100%)
B=2	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)	2/2 (1%)	0/2 (100%)
B=4	2/4 (5.23%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)	4/4 (0.01%)	0/4 (100%)
B=6	4/6 (0.127%)	0/6 (100%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	1/6 (46.9%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	0/6 (100%)	6/6 (1e-6)	0/6 (100%)
B=8	4/8 (5.02%)	0/8 (100%)	8/8 (1e-8)	0/8 (100%)	8/8 (1e-8)	0/8 (100%)	8/8 (1e-8)	0/8 (100%)	8/8 (1e-8)	0/8 (100%)	8/8 (1e-8)	0/8 (100%)

- DyePack effectively distinguishes contaminated models from clean ones.
- Using multiple backdoors lead to much lower FPRs than using a single backdoor.



With DyePack, you can flag contamination with provable FPR, requiring only the output text. Embed a DyePack to safeguard your next benchmark!